

**OPTET**  
**DELFT PLENARY MEETING**

AUEB

Network Economics  
and Services Group.

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# Trust Computational Model in Dynamic Context

Bayesian Inference based on Beta p.d.f.

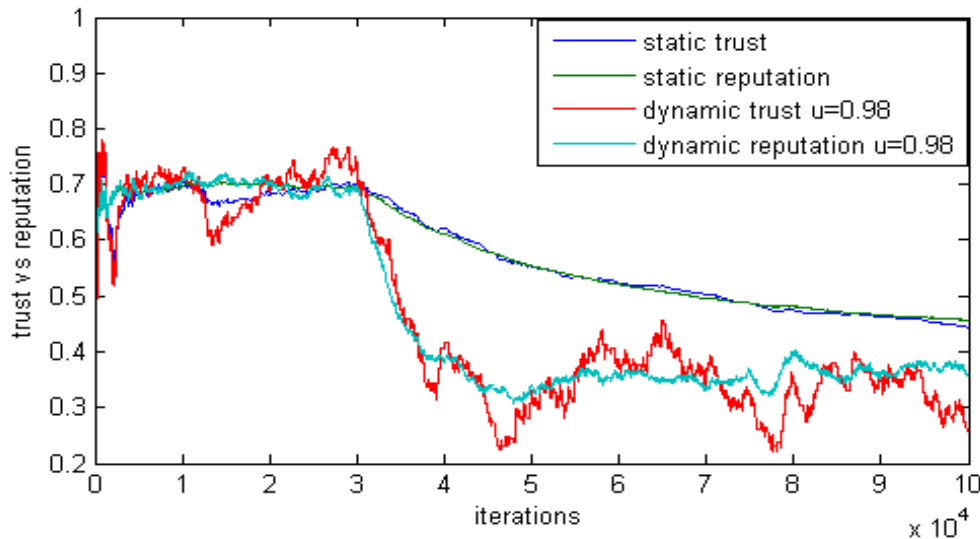
- **Static:** Observation equally weighted on estimation process.
  - ❑ Beta ( $\alpha, \beta$ ) : Increase the  $\alpha/\beta$  parameter if acceptable / unacceptable observation.
- **Dynamic:** More recent observations have a higher weight  $\rightarrow$  the impact of observations in distant past asymptotically vanishes.
  - ❑ Beta ( $\alpha, \beta$ ) : Update both parameters after each observation.  $s=1/0$  if acceptable / unacceptable

$$\alpha := u\alpha + s \quad \beta := u\beta + (1 - s) \quad u < 1$$

- **Trade-off:**
  - Static: (+) provides a more accurate estimation in cases of unchanged trustworthiness.
    - (-) needs a great number of observations to capture a possible change.
  - Dynamic: (+) captures faster any possible changes in trustworthiness
    - (-) suffers from oscillations around the estimated value.
- **Involving Marketplace :** Combine personal estimation and referrals from others.

# First Simulation Results

- ❑ Trustworthiness changes from 0.7  $\rightarrow$  0.35 at iteration 30K.
- ❑ Expected tradeoff appears between the two approaches.



- **Further issues:**

- 1) Trustworthiness of the marketplace mechanism  $\rightarrow$  reject inaccurate referrals.
- 2) Define the cost effective approach w.r.t priors and the number of iterations.
- 3) Define the optimal policy for the detection of a change in trustworthiness (window of last observations).

# Comparing Centralized vs Ad-hoc Trust Computational Models(1/2)

- ❑ The actual trustworthiness of a control is “ $\mu$ ”.
- ❑ Each agent has a **subjective estimation** for the trustworthiness of the control, based on **past “isolated”** observations :
  - ❑ Probability distribution function (Bayesian inference – Beta p.d.f.)
  - ❑ A point estimation (mean of Beta p.d.f. )
  - ❑ The average value of point estimations is “ $\mu$ ”.
- ❑ The agents are connected in a society. Each agent places weighted trust on neighbors, denoted by a row stochastic matrix (**normalization**).
- ❑ Studying how energy providers adopt controls for dealing with threats by *“learning from their neighbors”*.
- ❑ **Adding Marketplace** → most accurate estimation for “ $\mu$ ” (certificates).

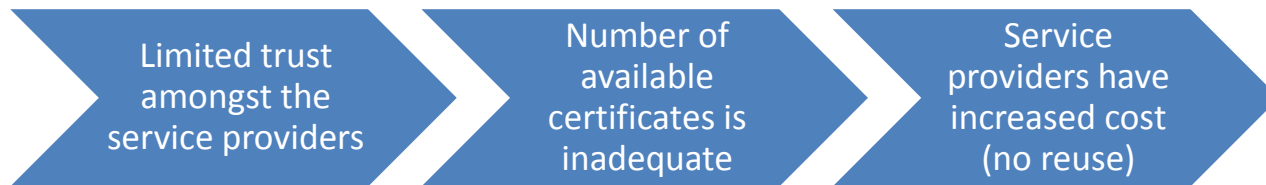
# Comparing Centralized vs Ad-hoc Trust Computational Models (2/2)

## Research Issues

- At each iteration:
  - ❑ Each agent revises the personal estimation.
  - ❑ The update equals a linear combination of personal and neighbors' estimations.
  
- Research Issues: **Consensus & Cost**
  - 1) Conditions in graph for converging to the same value (could be the wrong one...).
  
  - 2) Conditions in graph for converging to the same, **true** value: " $\mu$ ".
  
  - 3) How to insert the **marketplace** in the graph, s.t. the new consensus is closer to " $\mu$ "?
    - ❑ Redefine the trust matrix.
  
  - 4) How should the **marketplace** influence the beliefs of agents, consensus  $\rightarrow$  " $\mu$ "?
    - ❑ Consider a cost per unit of influence.

# Marketplace: The need for imposing minimum contribution schemes (1/2)

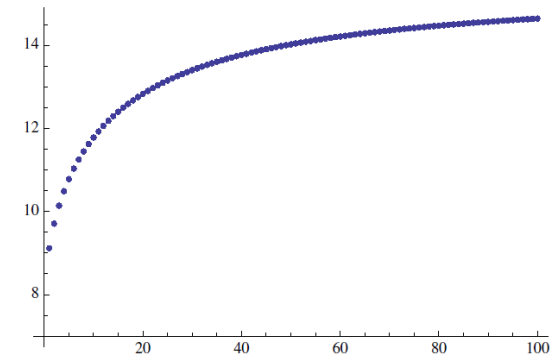
- Incentive problem
  - Free riding: service providers don't have the incentive to upload certificates to the Marketplace
- Consequences



- Proposed solution: impose a fixed minimum contribution to each provider → set of certificates is a *public good*
  - Incentive-compatible
  - Maximizes the social welfare
  - Simple to be enforced

# Marketplace: The need for imposing minimum contribution schemes (2/2)

- 2 substitute components are available:
  - Comp1 with known TW, e.g., mean  $\mu'$
  - Comp2 with a prior estimate of TW, e.g.,  $\mu \sim N[\mu_0, \sigma_0^2]$
- The benefit of providers from having  $n$  extra evidences of Comp2 is
  - concave if  $\mu > \mu'$
  - convex if  $\mu < \mu'$
- Approach:
  - Each provider truthfully announces its utility (as a function of the public good size)
  - Mechanism computes personalised minimum contribution levels



(a) For  $\sigma = 100$

# Optimal contracts as economic controls (1/2)



The theory of optimal contracts can help an AAL provider in designing contracts for each user category, so that:

- AAL provider maximizes its profits (second best), while
- each buyer has the incentive to choose the contract for its category

Users can be of 2 types based on their trust in PERS. Users'  $i$  utility is:  $\theta_i v(q) - T$

- $\theta_i$ : preferences of user type  $i$  (e.g., anxiety)
- $v(q)$ : value from placing  $q$  calls to the operator
- $T$ : payment asked by operator

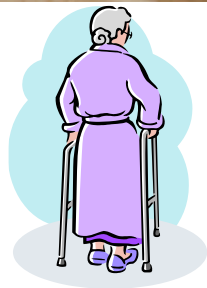
High trust in PERS

$\theta_H$

$\theta_H < \theta_L$

Low trust in PERS

$\theta_L$



$q_H$

$q_L$

Marginal cost of serving a call:  $C > 0$



Alarm call center operator has a belief that a person asking for service will be of:

- Low trust type:  $P_L$
- High Trust type :  $P_H = 1 - P_L$



# Optimal contracts as economic controls (2/2)

- Benchmark case: If operator knows the type of the user asking for service it can make a “take or leave it” offer (first-best) that would make the user indifferent (net benefit=0)
- In case of information asymmetry the operator maximizes its expected profit by:
  - offering a set of contracts  $(T_H, q_H)$ ,  $(T_L, q_L)$
  - and allowing users to select the most appropriate
  - Low-Trust user benefits from information asymmetry and achieves net benefit  $>0$ , while net benefit of High-Trust user=0
- Future work:
  - extend the model by including more than one service to the alarm call centre operator and
  - define contracts that incentivize service recipients to use the service more wisely (moral hazard model).